

Summary for Tutorial 5

QL

(Dated: November 18, 2008)

Keep in mind: You still need to read the lecture notes. My summary can't have everything in it. If there's an error, please email me.

I. RADIOCARBON DATING ACTIVITY MEASUREMENT

How many decays we have per unit time?

$$A(t) = \left| \frac{dN(t)}{dt} \right| = \text{Counts/unit time} \quad (1)$$

$$A(t) = \lambda \times N(t) \quad (2)$$

$$N(t) = N_0 \times e^{-\lambda t} \quad (3)$$

For ^{14}C : half life $T_{1/2} = 5730y$, decay constant $\lambda = \frac{\ln 2}{T_{1/2}} = 1.21 \times 10^{-4}/y$.

Statistical uncertainty = $\sqrt{\text{Counts}}$

II. RADIOCARBON DATING AMS

How many ^{14}C are there in the sample?

A. Tandem accelerator

Energy of the particle after pass through the accelerator:

$$E = (1 + q) \cdot V \quad (4)$$

with q the charge of the particle, V the terminal potential of the accelerator.

The radius of the trajectory is given by:

$$r = \frac{\sqrt{2mE}}{qB} \quad (5)$$

with m the mass of the particle, B the magnet field.

Example:

Given $V = 2MV$, $q = 3^+$, $B = 0.1T$, what's the radius

of ^{12}C ?

$$V = 2MV = 2 \times 10^6 V; \quad q = |q| \times 1.6 \times 10^{-19} C; \\ m = A \times 1.67 \times 10^{-27} kg$$

$$E = (1 + 3) \times 1.6 \times 10^{-19} C \times 2 \times 10^6 V = 1.28 \times 10^{-12} J(6) \\ r = \frac{\sqrt{2 \times 12 \times 1.67 \times 10^{-27} kg \times 1.28 \times 10^{-12} J}}{3 \times 1.6 \times 10^{-19} C \times 0.1 T} = 4.72 m(7)$$

Thus the radius of ^{12}C in the magnetic field is 4.72m.

B. Efficiency of AMS

Example

If the measured counts for ^{14}C is $N_{net} = 100 \pm 10$, and the efficiency is $\epsilon_c = 1\%$, what is the size of the sample?

Number of ^{14}C in the sample is:

$$N(^{14}\text{C}) = 100/1\% = 10^4 \quad (8)$$

Number of ^{12}C in the sample is:

$$N(^{12}\text{C}) = 10^4 / (1.3 \times 10^{-12}) = 7.69 \times 10^{15} \quad (9)$$

Mass of the sample:

$$m = \frac{7.69 \times 10^{15}}{6.022 \times 10^{23}} \times 12g = 1.5 \times 10^{-7} g \quad (10)$$

III. POTASSIUM ARGON DATING

^{40}K can decay to two different nuclei. 11% ^{40}K decays to ^{40}Ar .

$$N(^{40}\text{K}) = N_0 e^{-\lambda t} \quad (11)$$

$$N(^{40}\text{Ar}) = N_0 (1 - e^{-\lambda t}) \times 0.11 \quad (12)$$

Thus the ration is given by:

$$\frac{N(^{40}\text{Ar})}{N(^{40}\text{K})} = 0.11 \times (e^{\lambda t} - 1) \approx 5.82 \times 10^{-11} t \quad (13)$$

Thus we can infer the age of the sample by measuring the ratio.